

# Two-Factor Mixed and Within-Participants Designs

PSYC214: Statistics For Group Comparisons

Mark Hurlstone  
Lancaster University

Week 8

- PSYC214: Statistics for Group Comparisons
- m.hurlstone@lancaster.ac.uk
- A Two-Factor Mixed Design
  - Real-Data
  - Chi-Misog
  - ANOVA Tables
  - Simple Main Effects
  - Interaction Plot
  - Calculating F-Tests
- A Two-Factor Fully Within-Participants Design
  - Real-Data & Chi-Misog
  - ANOVA Tables
  - Simple Main Effects
  - Interaction Plot
  - Calculating F-Tests
- References

Notes

---

## Learning Objectives

- Two-factor mixed and within-participants designs
- Focus on procedures rather than how the analysis is calculated
- How to interpret ANOVA tables and graphs
- Handling significant main effects, and simple main effects, of factors with three or more levels

- PSYC214: Statistics for Group Comparisons
- m.hurlstone@lancaster.ac.uk
- A Two-Factor Mixed Design
  - Real-Data
  - Chi-Misog
  - ANOVA Tables
  - Simple Main Effects
  - Interaction Plot
  - Calculating F-Tests
- A Two-Factor Fully Within-Participants Design
  - Real-Data & Chi-Misog
  - ANOVA Tables
  - Simple Main Effects
  - Interaction Plot
  - Calculating F-Tests
- References

Notes

---

## Introduction

- We have now covered the three most mathematically straightforward designs:
  - 1 splitting total variability into between-group variability and within-group variability — one factor between-participants designs
  - 2 splitting within-group variability into between-participant variability and residual variability — one factor within-participants designs
  - 3 splitting between-group variability into main effect and interaction variability —  $2 \times 2$  between-participants design
- There is little new to learn from analysing more complicated designs by hand

- PSYC214: Statistics for Group Comparisons
- m.hurlstone@lancaster.ac.uk
- A Two-Factor Mixed Design
  - Real-Data
  - Chi-Misog
  - ANOVA Tables
  - Simple Main Effects
  - Interaction Plot
  - Calculating F-Tests
- A Two-Factor Fully Within-Participants Design
  - Real-Data & Chi-Misog
  - ANOVA Tables
  - Simple Main Effects
  - Interaction Plot
  - Calculating F-Tests
- References

Notes

---

## A Two-Factor Mixed Design

- Mixed design ANOVAs are particularly versatile and are often used in psychology
- These designs have at least one between-participants factor and at least one within-participants factor
- Allows the researcher to capitalise on the benefits of between- and within-participants designs within the same design
- Let's consider an example based on the Stroop task

- PSYC214: Statistics for Group Comparisons
- m.hurlstone@lancaster.ac.uk
- A Two-Factor Mixed Design
  - Real-Data
  - Chi-Misog
  - ANOVA Tables
  - Simple Main Effects
  - Interaction Plot
  - Calculating F-Tests
- A Two-Factor Fully Within-Participants Design
  - Real-Data & Chi-Misog
  - ANOVA Tables
  - Simple Main Effects
  - Interaction Plot
  - Calculating F-Tests
- References

Notes

---

## The Stroop Task

- In the Stroop task, participants must name the ink colour of a colour word as quickly as possible:
  - on **congruent trials**, the ink colour and colour name are consistent
  - on **incongruent trials**, the ink colour and colour name are inconsistent
- Stroop effect = longer RTs for incongruent, compared to congruent, trials
- A measure of **response inhibition**

### Congruent Trials



### Incongruent Trials



PSYC214:  
Statistics for Group  
Comparisons  
m.hurstone@  
lancaster.ac.uk

#### A Two-Factor Mixed Design

Raw Data  
Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

#### A Two-Factor Fully Within- Participants Design

Raw Data & Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

#### References

Notes

## Example of A Mixed Design

- A researcher wants to know if response inhibition is impaired in patients with Schizophrenia using the Stroop task
- She employs a  $2 \times 2$  mixed design:
  - patient group: healthy vs. schizophrenia
  - trial type: congruent vs. incongruent
- patient group is necessarily a between-participants factor
- trial type is a within-participants factor
- There are  $2 \times 2 = 4$  conditions; **two groups** of participants (healthy vs. schizophrenia) each complete two conditions of the experiment (congruent vs. incongruent trials)

PSYC214:  
Statistics for Group  
Comparisons  
m.hurstone@  
lancaster.ac.uk

#### A Two-Factor Mixed Design

Raw Data  
Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

#### A Two-Factor Fully Within- Participants Design

Raw Data & Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

#### References

Notes

## Hypothetical Data For Mixed-Design Stroop Experiment

		Factor B: Trial type (within participants)		
		Level B <sub>1</sub>	Level B <sub>2</sub>	
		congruent	incongruent	
Factor A:	Level A <sub>1</sub> healthy	P <sub>1</sub> 680	790	
	Group (between participants)	P <sub>2</sub>	616	746
P <sub>3</sub>		530	670	
P <sub>4</sub>		630	830	
P <sub>5</sub>		694	794	
Level A <sub>2</sub> schizophrenia		P <sub>6</sub> 630	852	
	P <sub>7</sub>	610	875	
	P <sub>8</sub>	602	863	
	P <sub>9</sub>	660	912	
	P <sub>10</sub>	673	928	

PSYC214:  
Statistics for Group  
Comparisons  
m.hurstone@  
lancaster.ac.uk

#### A Two-Factor Mixed Design

Raw Data  
Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

#### A Two-Factor Fully Within- Participants Design

Raw Data & Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

#### References

Notes

## Hypothetical Data For Mixed Design-Stroop Experiment

		Factor B: Trial type		
		Level B <sub>1</sub>	Level B <sub>2</sub>	Overall
		congruent	incongruent	
Factor A:	Level A <sub>1</sub> healthy	630	776	703
Group	Level A <sub>2</sub> schizophrenia	635	885	760
	Overall	632.5	830.5	

PSYC214:  
Statistics for Group  
Comparisons  
m.hurstone@  
lancaster.ac.uk

#### A Two-Factor Mixed Design

Raw Data  
Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

#### A Two-Factor Fully Within- Participants Design

Raw Data & Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

#### References

Notes

## Error Terms In A Mixed-Design ANOVA

- Recall that a between-participants design uses the within-group variance as its error term
- By contrast, a within-participants design uses the residual variance as its error term
- A mixed-design ANOVA produces two error terms:
  - one for the between-participants main effect
  - one for the within-participants main effect and the interaction
- You must be careful to ensure when reporting the ANOVA that the correct degrees of freedom are read from the table

PSYC214:  
Statistics for Group  
Comparisons

m.hurstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design

Real-Data

Cell Means

ANOVA Table

Simple Main Effects

Interaction Plot

Calculating F-Ratios

A Two-Factor

Fully Within-

Participants

Design

Real-Data & Cell Means

ANOVA Table

Simple Main Effects

Interaction Plot

Calculating F-Ratios

References

Navigation icons

Notes

## ANOVA Table For Mixed-Design Stroop Experiment

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
A (group)	19531.250	1	19531.250	4.307	0.072
Error S/A (Bet-ss)	36281.000	8	4535.125		
B (trial type)	187211.250	1	187211.250	411.793	< .001
A × B	16531.250	1	16531.250	36.362	< .001
Error B × S/A	3637.000	8	454.625		

- One error term is labelled *Error S/A (Bet-ss)* and has been used to calculate the *F* ratio for the between-participants factor
- Error B × S/A* has been used to calculate the *F* ratio for every component linked to factor B—the within-participants factor and interaction

PSYC214:  
Statistics for Group  
Comparisons

m.hurstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design

Real-Data

Cell Means

ANOVA Table

Simple Main Effects

Interaction Plot

Calculating F-Ratios

A Two-Factor

Fully Within-

Participants

Design

Real-Data & Cell Means

ANOVA Table

Simple Main Effects

Interaction Plot

Calculating F-Ratios

References

Navigation icons

Notes

## ANOVA Table For Mixed-Design Stroop Experiment

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
A (group)	19531.250	1	19531.250	4.307	0.072
Error S/A (Bet-ss)	36281.000	8	4535.125		
B (trial type)	187211.250	1	187211.250	411.793	< .001
A × B	16531.250	1	16531.250	36.362	< .001
Error B × S/A	3637.000	8	454.625		

- One error term is labelled *Error S/A (Bet-ss)* and has been used to calculate the *F* ratio for the between-participants factor
- Error B × S/A* has been used to calculate the *F* ratio for every component linked to factor B—the within-participants factor and interaction

PSYC214:  
Statistics for Group  
Comparisons

m.hurstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design

Real-Data

Cell Means

ANOVA Table

Simple Main Effects

Interaction Plot

Calculating F-Ratios

A Two-Factor

Fully Within-

Participants

Design

Real-Data & Cell Means

ANOVA Table

Simple Main Effects

Interaction Plot

Calculating F-Ratios

References

Navigation icons

Notes

## ANOVA Table For Mixed-Design Stroop Experiment

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
A (group)	19531.250	1	19531.250	4.307	0.072
Error S/A (Bet-ss)	36281.000	8	4535.125		
B (trial type)	187211.250	1	187211.250	411.793	< .001
A × B	16531.250	1	16531.250	36.362	< .001
Error B × S/A	3637.000	8	454.625		

- One error term is labelled *Error S/A (Bet-ss)* and has been used to calculate the *F* ratio for the between-participants factor
- Error B × S/A* has been used to calculate the *F* ratio for every component linked to factor B—the within-participants factor and interaction

PSYC214:  
Statistics for Group  
Comparisons

m.hurstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design

Real-Data

Cell Means

ANOVA Table

Simple Main Effects

Interaction Plot

Calculating F-Ratios

A Two-Factor

Fully Within-

Participants

Design

Real-Data & Cell Means

ANOVA Table

Simple Main Effects

Interaction Plot

Calculating F-Ratios

References

Navigation icons

Notes

## Simple Main Effects Table For Mixed-Design Stroop Experiment

- There are different approaches to testing simple main effects in mixed designs
- The simplest approach uses **pooled error terms**
- We begin by calculating the between-group variance for each simple main effect
- The calculations are identical to those used for the between-participants design (see Week 7 lecture slides)
- Each pair of simple main effects is tested for significance using the same error term (hence pooled error term approach)

Navigation icons

PSYC214: Statistics for Group Comparisons  
 m.hurlstone@lancaster.ac.uk

A Two-Factor Mixed Design  
 Real Data  
 Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F ratios

A Two-Factor Fully Within-Participants Design  
 Real Data & Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F ratios

References

Notes

## Simple Main Effects Table For Mixed-Design Stroop Experiment

- The error term for testing the significance of the between-participant effects is the pooled within-group variance for the four cells
- This is calculated identically to a fully between-participants design  $\{SS_{S/AB} = [Y] - [AB]; df_{S/AB} = ab(s - 1)\}$
- This is used to test the significance of the two simple main effects of the between-participants factor:
  - group at congruent
  - group at incongruent

Navigation icons

PSYC214: Statistics for Group Comparisons  
 m.hurlstone@lancaster.ac.uk

A Two-Factor Mixed Design  
 Real Data  
 Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F ratios

A Two-Factor Fully Within-Participants Design  
 Real Data & Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F ratios

References

Notes

## Simple Main Effects Table For Mixed-Design Stroop Experiment

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
Group at					
congruent	62.500	1	62.500	0.014	0.909
incongruent	36000.00	1	36000.00	7.938	0.023
Error term	36281.00	8	4535.125		
Trial type at					
healthy	46240.000	1	46240.000	101.710	< .001
schizophrenia	157502.500	1	157502.500	346.445	< .001
Error term	3637.000	8	454.625		

Navigation icons

PSYC214: Statistics for Group Comparisons  
 m.hurlstone@lancaster.ac.uk

A Two-Factor Mixed Design  
 Real Data  
 Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F ratios

A Two-Factor Fully Within-Participants Design  
 Real Data & Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F ratios

References

Notes

## Simple Main Effects Table For Mixed-Design Stroop Experiment

- The other error term is the within-participants factor error term from the initial ANOVA (*Error B × S/A*)
- This is used to test the two within-participants simple main effects:
  - trial type at healthy
  - trial type at schizophrenia

Navigation icons

PSYC214: Statistics for Group Comparisons  
 m.hurlstone@lancaster.ac.uk

A Two-Factor Mixed Design  
 Real Data  
 Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F ratios

A Two-Factor Fully Within-Participants Design  
 Real Data & Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F ratios

References

Notes



## Simple Main Effects Table For Mixed-Design Stroop Experiment

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
<b>Group at</b>					
congruent	62.500	1	62.500	0.014	0.909
incongruent	36000.00	1	36000.00	7.938	0.023
Error term	36281.00	8	4535.125		
<b>Trial type at</b>					
healthy	46240.000	1	46240.000	101.710	< .001
schizophrenia	157502.500	1	157502.500	346.445	< .001
Error term	3637.000	8	454.625		

PSYC214:  
Statistics for Group  
Comparisons

m.hurlstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design

Real Data

Cell Means

ANOVA Table

Simple Main Effects

Interaction Plot

Calculating F-tests

A Two-Factor  
Fully Within-  
Participants  
Design

Real Data & Cell Means

ANOVA Table

Simple Main Effects

Interaction Plot

Calculating F-tests

References

Notes

## Simple Main Effects Table For Mixed-Design Stroop Experiment

- An alternative to this approach would be to calculate a separate *t*-test for each pair of means being compared
- We would use independent-samples *t*-tests to test the simple main effects of the between-participants factor
- We would use repeated-measures *t*-tests to test the simple main effects of the within-participants factor

PSYC214:  
Statistics for Group  
Comparisons

m.hurlstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design

Real Data

Cell Means

ANOVA Table

Simple Main Effects

Interaction Plot

Calculating F-tests

A Two-Factor  
Fully Within-  
Participants  
Design

Real Data & Cell Means

ANOVA Table

Simple Main Effects

Interaction Plot

Calculating F-tests

References

Notes

## Simple Main Effects Table For Mixed-Design Stroop Experiment

- Once you have calculated the simple main effects, generate an interaction plot
- Locate the simple main effects in the graph to facilitate interpretation of the interaction

PSYC214:  
Statistics for Group  
Comparisons

m.hurlstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design

Real Data

Cell Means

ANOVA Table

Simple Main Effects

Interaction Plot

Calculating F-tests

A Two-Factor  
Fully Within-  
Participants  
Design

Real Data & Cell Means

ANOVA Table

Simple Main Effects

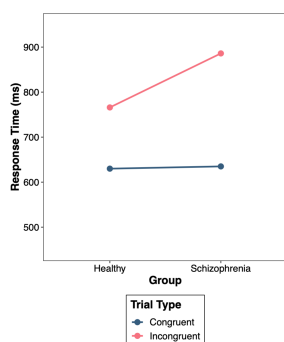
Interaction Plot

Calculating F-tests

References

Notes

## Interaction Plot



PSYC214:  
Statistics for Group  
Comparisons

m.hurlstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design

Real Data

Cell Means

ANOVA Table

Simple Main Effects

Interaction Plot

Calculating F-tests

A Two-Factor  
Fully Within-  
Participants  
Design

Real Data & Cell Means

ANOVA Table

Simple Main Effects

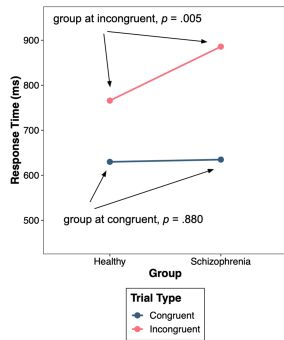
Interaction Plot

Calculating F-tests

References

Notes

## Interaction Plot



PSYC214: Statistics for Group Comparisons  
m.hurlstone@lancaster.ac.uk

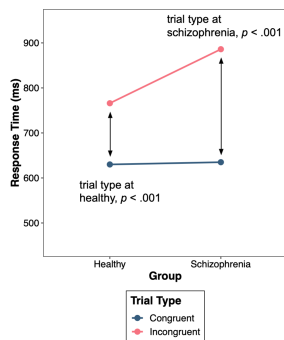
A Two-Factor Mixed Design  
Real Data  
Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F Values

A Two-Factor Fully Within-Participants Design  
Real Data & Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F Values

References

Notes

## Interaction Plot



PSYC214: Statistics for Group Comparisons  
m.hurlstone@lancaster.ac.uk

A Two-Factor Mixed Design  
Real Data  
Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F Values

A Two-Factor Fully Within-Participants Design  
Real Data & Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F Values

References

Notes

## Simple Main Effects Table For Mixed-Design Stroop Experiment

- Once you have a graph and have calculated the simple main effects, write out the various effects as you were shown in the Week 6 lab session
- This involves reporting the  $F$  values for each simple main effect and stating the direction of the significant differences
- Once the significant effects have been identified, they must be interpreted
- Write a couple of sentences to describe the nature of the interaction (see the Week 7 lab session for an example)

PSYC214: Statistics for Group Comparisons  
m.hurlstone@lancaster.ac.uk

A Two-Factor Mixed Design  
Real Data  
Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F Values

A Two-Factor Fully Within-Participants Design  
Real Data & Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F Values

References

Notes

## What If The Design Has Three or More Levels In Either Factor?

- If the interaction is not significant, any significant main effects for factors with three or more levels will need to be followed up with planned comparisons ( $t$ -tests) or post-hoc tests (Tukey test)
- When the interaction is significant, the simple main effects for a factor with three or more levels will need to be followed up with planned comparisons or post-hoc tests
- In both circumstances, planned comparisons will often be preferable
- Make sure you use the right type (independent samples vs. repeated measures) for the effect you are testing

PSYC214: Statistics for Group Comparisons  
m.hurlstone@lancaster.ac.uk

A Two-Factor Mixed Design  
Real Data  
Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F Values

A Two-Factor Fully Within-Participants Design  
Real Data & Cell Means  
ANOVA Tables  
Simple Main Effects  
Interaction Plot  
Calculating F Values

References

Notes

## Calculating $F$ ratios

- The book chapter in the recommended reading includes a demonstration of how to calculate the  $F$  ratios for a mixed design by hand
- Only study this if you are curious, it is not something you will be assessed upon
- The procedure is very similar to that used when we calculated  $F$  ratios for a two-factor between-participant design—it uses the same basic ratios (plus one new ratio)

PSYC214:  
Statistics for Group  
Comparisons  
m.hurstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design  
Raw Data  
Cell Means  
ANOVA Table  
Simple Main Effects  
Interaction PDI  
Calculating  $F$  ratios

A Two-Factor  
Fully Within-  
Participants  
Design  
Raw Data & Cell Means  
ANOVA Table  
Simple Main Effects  
Interaction PDI  
Calculating  $F$  ratios

References

Notes

## A Two-Factor Fully Within-Participants Design

- A researcher wants to know if the size of the Stroop effect decreases with practice
- She employs a  $2 \times 3$  fully within-participants design:
  - trial type: congruent vs. incongruent
  - block: 1 vs. 2 vs. 3
- Making *trial type* within-participants means we can establish each participant's susceptibility to the Stroop effect
- block* must necessarily be a within-participants factor, as it requires experience with the task
- There are  $2 \times 3 = 6$  conditions; a single group of participants completes each condition

PSYC214:  
Statistics for Group  
Comparisons  
m.hurstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design  
Raw Data  
Cell Means  
ANOVA Table  
Simple Main Effects  
Interaction PDI  
Calculating  $F$  ratios

A Two-Factor  
Fully Within-  
Participants  
Design  
Raw Data & Cell Means  
ANOVA Table  
Simple Main Effects  
Interaction PDI  
Calculating  $F$  ratios

References

Notes

## Hypothetical Data For Fully Within-Participants Design Stroop Experiment

	$A_1$ congruent			$A_2$ incongruent		
	$B_1$ block 1	$B_2$ block 2	$B_3$ block 3	$B_1$ block 1	$B_2$ block 2	$B_3$ block 3
$P_1$	700	600	550	910	700	625
$P_2$	600	550	575	850	650	650
$P_3$	480	590	693	720	685	743
$P_4$	630	690	597	830	790	600
$P_5$	720	730	650	845	770	680
Means	626.00	632.00	613.00	831.00	719.00	659.60

PSYC214:  
Statistics for Group  
Comparisons  
m.hurstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design  
Raw Data  
Cell Means  
ANOVA Table  
Simple Main Effects  
Interaction PDI  
Calculating  $F$  ratios

A Two-Factor  
Fully Within-  
Participants  
Design  
Raw Data & Cell Means  
ANOVA Table  
Simple Main Effects  
Interaction PDI  
Calculating  $F$  ratios

References

Notes

## ANOVA Table For Fully Within-Participants Design Stroop Experiment

Source	Sum of Squares	Degrees of Freedom	Mean Square	$F$	$P$
$A$ (trial type)	95541.63	1	95541.63	68.124	< .001
Error $A \times P$	5609.87	4	1402.47		
$B$ (block)	42821.60	2	21410.80	2.128	0.182
Error $B \times P$	80503.40	8	10062.93		
$A \times B$	33872.27	2	16936.13	53.537	< .001
Error $A \times B \times P$	2530.73	8	316.34		
$P$ (participants)	28847.20	4	7211.800		

- Each effect has its own error term directly underneath it, which makes locating the degrees of freedom easier

PSYC214:  
Statistics for Group  
Comparisons  
m.hurstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design  
Raw Data  
Cell Means  
ANOVA Table  
Simple Main Effects  
Interaction PDI  
Calculating  $F$  ratios

A Two-Factor  
Fully Within-  
Participants  
Design  
Raw Data & Cell Means  
ANOVA Table  
Simple Main Effects  
Interaction PDI  
Calculating  $F$  ratios

References

Notes

## ANOVA Table For Fully Within-Participants Design Stroop Experiment

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
A (trial type)	95541.63	1	95541.63	68.124	< .001
Error A × P	5609.87	4	1402.47		
B (block)	42821.60	2	21410.80	2.128	0.182
Error B × P	80503.40	8	10062.93		
A × B	33872.27	2	16936.13	53.537	< .001
Error A × B × P	2530.73	8	316.34		
P (participants)	28847.20	4	7211.800		

- Each effect has its own error term directly underneath it, which makes locating the degrees of freedom easier

PSYC214: Statistics for Group Comparisons  
 m.hurlstone@lancaster.ac.uk

A Two-Factor Mixed Design  
 Real Data  
 Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F-ratios

A Two-Factor Fully Within-Participants Design  
 Real Data & Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F-ratios

References

Notes

## Simple Main Effects Table For Fully Within-Participants Design Stroop Experiment

- To test the simple main effects, we calculate the between-group variances as we did in our Week 7 lecture
- The error terms to use are those from the original ANOVA table
- Thus, for the simple main effects of factor A (trial type) at B<sub>1</sub>, B<sub>2</sub>, and B<sub>3</sub> the error term for testing factor A could be used (Error A × P)
- For the simple main effects of factor B (block) at A<sub>1</sub> and A<sub>2</sub> the error term for testing factor B could be used (Error B × P)

PSYC214: Statistics for Group Comparisons  
 m.hurlstone@lancaster.ac.uk

A Two-Factor Mixed Design  
 Real Data  
 Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F-ratios

A Two-Factor Fully Within-Participants Design  
 Real Data & Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F-ratios

References

Notes

## Simple Main Effects Table For Fully Within-Participants Design Stroop Experiment

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
Trial type at					
block 1	105062.50	1	105062.50	74.913	< .001
block 2	18922.50	1	18922.50	13.492	0.021
block 3	5428.90	1	5428.90	3.871	0.121
Error term	5609.87	4	1402.47		
Block at					
congruent	943.33	2	471.67	0.047	0.954
incongruent	75750.53	2	37875.27	3.764	0.041
Error term	65457.33	8	10062.93		

PSYC214: Statistics for Group Comparisons  
 m.hurlstone@lancaster.ac.uk

A Two-Factor Mixed Design  
 Real Data  
 Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F-ratios

A Two-Factor Fully Within-Participants Design  
 Real Data & Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F-ratios

References

Notes

## Simple Main Effects Table For Fully Within-Participants Design Stroop Experiment

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
Trial type at					
block 1	105062.50	1	105062.50	74.913	< .001
block 2	18922.50	1	18922.50	13.492	0.021
block 3	5428.90	1	5428.90	3.871	0.121
Error term	5609.87	4	1402.47		
Block at					
congruent	943.33	2	471.67	0.047	0.954
incongruent	75750.53	2	37875.27	3.764	0.041
Error term	65457.33	8	10062.93		

PSYC214: Statistics for Group Comparisons  
 m.hurlstone@lancaster.ac.uk

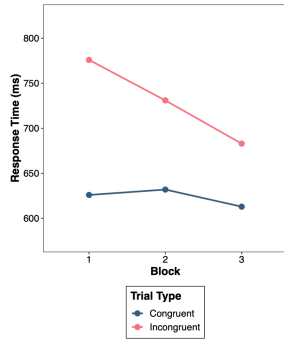
A Two-Factor Mixed Design  
 Real Data  
 Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F-ratios

A Two-Factor Fully Within-Participants Design  
 Real Data & Cell Means  
 ANOVA Table  
 Simple Main Effects  
 Interaction Plot  
 Calculating F-ratios

References

Notes

## Interaction Plot



PSYC214: Statistics for Group Comparisons  
m.hurstone@lancaster.ac.uk

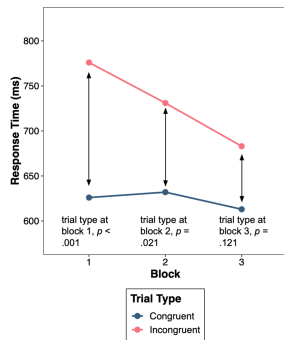
A Two-Factor Mixed Design  
Real Data  
Chi-Msqp  
ANOVA Table  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

A Two-Factor Fully Within-Participants Design  
Real Data & Cell Means  
ANOVA Table  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

References

Notes

## Interaction Plot



PSYC214: Statistics for Group Comparisons  
m.hurstone@lancaster.ac.uk

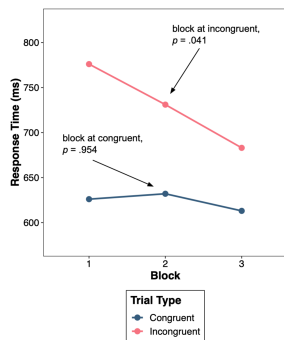
A Two-Factor Mixed Design  
Real Data  
Chi-Msqp  
ANOVA Table  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

A Two-Factor Fully Within-Participants Design  
Real Data & Cell Means  
ANOVA Table  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

References

Notes

## Interaction Plot



PSYC214: Statistics for Group Comparisons  
m.hurstone@lancaster.ac.uk

A Two-Factor Mixed Design  
Real Data  
Chi-Msqp  
ANOVA Table  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

A Two-Factor Fully Within-Participants Design  
Real Data & Cell Means  
ANOVA Table  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

References

Notes

## Follow Up Tests For Simple Main effects Of Factors With Three Or More Levels

- In this instance, one of the simple main effects of our factor with three levels (block at incongruent) was significant
- We therefore need to perform follow up tests (planned comparisons or post-hoc tests) to determine where the differences are located
- I recommend using planned comparisons where possible
- We will evaluate the simple main effect of block at incongruent trials by performing two repeated-measures  $t$ -tests comparing block 1 vs. block 2 and block 2 vs. block 3 (i.e., planned comparisons)

PSYC214: Statistics for Group Comparisons  
m.hurstone@lancaster.ac.uk

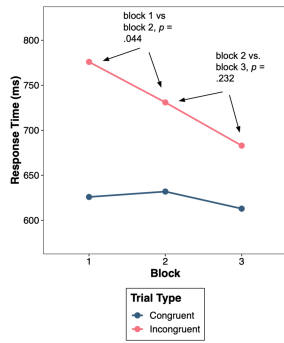
A Two-Factor Mixed Design  
Real Data  
Chi-Msqp  
ANOVA Table  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

A Two-Factor Fully Within-Participants Design  
Real Data & Cell Means  
ANOVA Table  
Simple Main Effects  
Interaction Plot  
Calculating F-ratios

References

Notes

## Interaction Plot



PSYC214:  
Statistics for Group  
Comparisons

m.hurstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design

Real Data  
Chi-Msqp  
ANOVA Tables  
Single Main Effects  
Interaction Plot  
Calculating F-Ratios

A Two-Factor  
Fully Within-  
Participants  
Design

Real Data & Cell Means  
ANOVA Tables  
Single Main Effects  
Interaction Plot  
Calculating F-Ratios

References

Notes

## Calculating F ratios

- The book chapter in the recommended reading includes a demonstration of how to calculate the  $F$  ratios for a within-participants design by hand
- Only study this if you are curious, it is not something you will be assessed upon
- The procedure is very similar to that used when we calculated  $F$  ratios for a two-factor between-participant design—it uses the same basic ratios (plus one new ratio)

PSYC214:  
Statistics for Group  
Comparisons

m.hurstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design

Real Data  
Chi-Msqp  
ANOVA Tables  
Single Main Effects  
Interaction Plot  
Calculating F-Ratios

A Two-Factor  
Fully Within-  
Participants  
Design

Real Data & Cell Means  
ANOVA Tables  
Single Main Effects  
Interaction Plot  
Calculating F-Ratios

References

Notes

## A Note On The Sphericity Assumption

- The sphericity assumption extends to within-participants factorial designs with factors containing three or more levels
- It also applies to within-participant factors with three or more levels in mixed designs
- R will apply the Greenhouse and Geisser correction if the sphericity assumption is violated
- We'll cover this in more detail in next week's lab

PSYC214:  
Statistics for Group  
Comparisons

m.hurstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design

Real Data  
Chi-Msqp  
ANOVA Tables  
Single Main Effects  
Interaction Plot  
Calculating F-Ratios

A Two-Factor  
Fully Within-  
Participants  
Design

Real Data & Cell Means  
ANOVA Tables  
Single Main Effects  
Interaction Plot  
Calculating F-Ratios

References

Notes

## Additional Resources

- The R code for all plots generated in this lecture (minus annotations) has been uploaded with these slides to the Week 8 lecture folder (R Plots For Lecture 8.R)

PSYC214:  
Statistics for Group  
Comparisons

m.hurstone@  
lancaster.ac.uk

A Two-Factor  
Mixed Design

Real Data  
Chi-Msqp  
ANOVA Tables  
Single Main Effects  
Interaction Plot  
Calculating F-Ratios

A Two-Factor  
Fully Within-  
Participants  
Design

Real Data & Cell Means  
ANOVA Tables  
Single Main Effects  
Interaction Plot  
Calculating F-Ratios

References

Notes

## In Next Week's Lab ...

- Running a  $2 \times 3$  mixed/within-participants ANOVA in R
- Follow-up tests for factors with more than two levels

PSYC214:  
Statistics for Group  
Comparisons  
m.hurlstone@  
lancaster.ac.uk

### A Two-Factor Mixed Design

Real Data  
Chi-Msqp  
ANOVA Table  
Simple Main Effects  
Interaction Plot  
Calculating F ratios

### A Two-Factor Fully Within- Participants Design

Real Data & Cell Means  
ANOVA Table  
Simple Main Effects  
Interaction Plot  
Calculating F ratios

### References

Navigation icons

Notes

---

## References

Roberts, M. J., & Russo, R. (1999, Chapter 11). *A student's guide to Analysis of Variance*. Routledge: London.

PSYC214:  
Statistics for Group  
Comparisons  
m.hurlstone@  
lancaster.ac.uk

### A Two-Factor Mixed Design

Real Data  
Chi-Msqp  
ANOVA Table  
Simple Main Effects  
Interaction Plot  
Calculating F ratios

### A Two-Factor Fully Within- Participants Design

Real Data & Cell Means  
ANOVA Table  
Simple Main Effects  
Interaction Plot  
Calculating F ratios

### References

Navigation icons

Notes

---

Notes

---

Notes

---